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# **Wind Tunnel Wall Effects on the Flow around a 76/40-deg Double-Delta Wing**

by

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### **Abstract**

Surface-pressure data of a 76/40-deg double-delta wing tested in the BART wind tunnel at NASA LaRC have been corrected for tunnel wall and support interference effects. The correction is shown to improve the correlation between the computed and measured pressure data. Overviews are given of existing tunnel wall correction procedures for wings with leading-edge vortex separation and of studies that investigate the effect of tunnel walls on the vortex burst location.

# Contents

<b>1</b>	<b>Nomenclature</b>	<b>2</b>
<b>2</b>	<b>Introduction</b>	<b>3</b>
<b>3</b>	<b>BART Experiment</b>	<b>5</b>
3.1	Wind Tunnel . . . . .	5
3.2	Model . . . . .	5
3.3	Experimental Tests . . . . .	5
3.4	Test Results . . . . .	6
<b>4</b>	<b>Wind Tunnel Wall Corrections</b>	<b>9</b>
4.1	Tunnel Wall Effects . . . . .	9
4.2	Overview of Wall Correction Methods . . . . .	9
4.3	Details of Wall Correction Methods . . . . .	10
4.3.1	Method of Garner and Rogers . . . . .	10
4.3.2	Method of Frink . . . . .	11
4.3.3	Wake Blockage Correction Method . . . . .	12
4.3.4	Pressure Signature Method . . . . .	13
4.3.5	Numerical Simulations . . . . .	13
4.4	Discussion . . . . .	13
<b>5</b>	<b>Corrections applied to BART Test Data</b>	<b>15</b>
5.1	Blockage Effect . . . . .	15
5.2	Lift Effect . . . . .	17
5.3	Wall Corrections applied to $C_p$ -Distributions . . . . .	17
<b>6</b>	<b>Tunnel Wall Effects on Vortex Breakdown; A Literature Survey</b>	<b>19</b>
<b>7</b>	<b>Conclusions and Recommendations</b>	<b>21</b>
<b>8</b>	<b>Acknowledgements</b>	<b>21</b>
<b>9</b>	<b>References</b>	<b>22</b>
<b>10</b>	<b>Figures</b>	<b>24</b>

# 1 Nomenclature

$B$	tunnel span
$b$	wing span
$c$	root chord length, = 2.406 m (16 in.)
$\bar{c}$	mean aerodynamic chord
$C_D$	drag coefficient
$C_{Ds}$	separation drag coefficient
$C_L$	lift coefficient
$C_N$	normal force coefficient
$C_p$	static pressure coefficient, = $(p - p_\infty)/q_\infty$
$C_{pt}$	total pressure coefficient, = $(p_t - p_\infty)/q_\infty$
$H$	tunnel height
$M$	freestream Mach number
$p$	static pressure
$p_t$	total pressure
$p_\infty$	freestream static pressure
$q_\infty$	freestream dynamic pressure
$R_b$	$b/B$
$R_t$	$H/B$
$Re$	Reynolds number, based on root chord length
$s$	local wing semispan
$x, y, z$	coordinates of wing axes system, origin at apex
$\alpha, AOA$	angle of attack
$\Lambda$	leading-edge sweep angle

## 2 Introduction

Modern NAVY fighter aircraft are designed to rely on the enhanced lift generated by vortex flow to enable high maneuverability. Vortical flows are part of the overall flow structure of these aircraft. Current designs result in the shedding of vortices from various locations on the aircraft including the forebody, moderate to highly swept wing leading edges, strakes and leading edge extensions, and the junction of aerodynamic surfaces with each other and the fuselage. The shedding, interaction and breakdown of these vortices are highly sensitive to both the aircraft geometry and the flow conditions. In addition to producing the benefits of enhanced lift and maneuverability, the vortical flow also causes serious departure and structural fatigue problems, e.g., the vortex tail buffet phenomenon of F/A-18 aircraft. Techniques for controlling the trajectory, strength and breakdown processes of the vortices may not only alleviate the problems generated by this flow phenomenon, but also enhance the existing controllability, maneuverability and agility of the aircraft.

In a numerical study, Kern [1] of NAWC (Naval Air Warfare Center) investigated the effects of small deployable fillets at the junction of the strake/wing leading edge of a cropped double-delta wing. The strake and wing leading edges had a sweep angle of 76 and 40 deg, respectively, forming a baseline planform representative of highly-maneuverable aircraft. The fillets investigated had a linear, parabolic and diamond shape. The numerical predictions indicated that the fillets do affect the shedding process at the junction of the strake/wing leading edge and thus the trajectories, vortex interaction and breakdown of the vortices over the double-delta wing. At an angle of attack of 10 deg., which is in the range of Naval aircraft approaching a carrier for landing, the fillets were predicted to shift the vortex structure outboard. This potential may lead to a method of alleviating tail buffet by deflecting the vortices away from the tail surfaces. Through asymmetric deployment of the fillets, additional lateral-directional control may be realized. At an angle of attack of 22.5 deg, which is the angle of attack at which Naval aircraft maneuver, the fillets delayed vortex breakdown by providing a favorable vortex interaction. The delay in breakdown enhances the lift with a slight improvement in lift-to-drag ratio.

For a validation of the numerical predictions, experimental tests are necessary to generate data on the effect of fillets on the vortex flowfield, induced wing surface pressures and forces and moments at various angles of attack and sideslip. To obtain this data, NAWC constructed a 76/40-deg double-delta wing model (Fig. 1). In the frame of a cooperative research effort between the NASA LaRC (Langley Research Center) and NAWC, this wing was tested at different test conditions in the LaRC 8-ft tunnel, the 7-ft by 10-ft tunnel and the BART (Basic Aerodynamic Research Tunnel).

The testings in BART were carried out on the baseline configuration of the double-delta wing (so without fillets) and included flow visualization tests, surface pressure recordings and flowfield surveys. The data were used to validate solutions of the thin-layer Navier-Stokes equations for fully laminar flow obtained by Kern. The study, reported by Verhaagen, et al, [2] showed the solutions to well predict the behavior of the flow on and off the upper surface of the baseline double-delta wing. However, large differences were found between the predicted and measured upper-surface pressure distributions. These

differences were due to the fact that the tunnel wall and model support interference effects were not fully taken into account, both in the testings and the predictions.

Interference of the tunnel walls and model support results into an increase in dynamic pressure of the flow around the wing due to solid and wake blockage. In addition, lift interference and streamline curvature effects change the angle of attack.

The objective of the study described in the present report was to apply wall and support interference corrections to the test data and to compare the corrected data with the numerical solutions. In addition, to discuss published data on the effect of tunnel walls on the breakdown of leading-edge vortex cores. A summary of the BART test setup and results is given in section 3. An overview of existing wall interference correction methods is given in section 4, while the effect of the corrections on the test data and on the comparison with the solutions is discussed in section 5. Finally, the effect of tunnel walls on the vortex core breakdown location is discussed in section 6.

The present study has been conducted in the frame of EOARD Special Contract Program SPC 96-4008.

### 3 BART Experiment

#### 3.1 Wind Tunnel

The tests were carried out in the BART of the NASA LaRC. This is a subsonic, open-return wind tunnel with a test section 0.71 m high, 1.02 m wide and 3.05 m long (Fig. 2). The variation in longitudinal turbulence intensity ranges from approximately 0.03% at an air speed of 15 m/sec to 0.09% at an air speed of 48 m/sec. Further details of the wind tunnel facility can be found in reference [3] by Sellers and Kjelgaard.

#### 3.2 Model

The model was a stainless steel 76/40-deg swept double-delta wing designed and provided by NAWC (Fig. 1). The model had a chord length of 0.406 m (16 inches), a span of 0.415 m and thickness of 9.53 mm. The leading-edge kink was situated at 52% chord and the wing tip was cropped from the 84% chordwise station. The sharp leading and trailing edges of the model were broken and rounded to a diameter of 0.13 mm (0.005 in.). The under surface was beveled at 20 deg over a width of 26.16 mm. The kink section was capable of allowing fillets of different leading edge geometry to be installed. In the BART only the baseline configuration with straight strake and wing leading edges was tested. The left upper surface of the model was equipped with 48 pressure orifices of 0.25 mm (0.010 in.) diameter. Ten orifices were drilled in a spanwise row at 25% chord, while 19 orifices were drilled both at 75% and 90% chord. The pressure tubes exited the model at its lower surface. The model was supported in the tunnel by an internal-balance sting attached to its lower surface (Fig. 3). A fairing was fitted to the lower surface of the model to cover the balance block and the pressure tubes. The angle of attack of the model was set with a remotely controlled sting/post support. The angle of attack was monitored with an accelerometer mounted on the sting at a short distance behind the trailing edge of the model. The maximum uncertainty in the angle of attack reading was 0.03 deg.

#### 3.3 Experimental Tests

A smoke/laserlight-sheet technique was used to visualize the structure of the vortex flow and to study probe/vortex interference effects. A single column of vaporized propylene glycol was introduced upstream of the tunnel inlet and positioned such that it could be entrained into the vortices generated by the model. A 6-Watt Argon-ion laser and a twin-mirrored galvanometer laserlight-sheet generator were used to illuminate the propylene glycol particles and thus the vortices. Two cameras were set at different viewing angles to capture the flow in planes both normal and parallel to the surface of the model. The laserlight-sheet technique was used at angles of attack ranging from 5 to 22.5 deg and a Reynolds number ( $Re$ ) of mostly 0.5 million ( $M$ ).

Surface flow visualization was used to determine the location of stagnation, attachment and separation lines in the boundary layer pattern on the upper surface of the model. This pattern was visualized using a mixture of titanium dioxide ( $TiO_2$ ) and kerosene.



The surface flow pattern was investigated at angles of attack ranging from  $-10$  to  $22.5$  deg and  $Re = 0.5, 1.0$  and  $1.5$  M.

The distribution of the upper-surface  $C_p$  at the 25, 75 and 90% chordwise stations was measured at angles of attack ranging from  $-5.0$  to  $25.0$  deg and  $Re = 1.0$  M. To study the effect of the Reynolds number on  $C_p$ , at  $\alpha = 10$  and  $22.5$  deg pressures were acquired at  $Re$  ranging from  $0.5$  to  $1.5$  M. While preparing the model for the surface pressure measurements, 2 of the 10 pressure ports at 25% chord were found to be unreliable. Therefore, these ports were not used during the testings. The remaining 46 pressure ports in the model were connected to transducers with a maximum range of  $\pm 1.0$  p.s.i. and an uncertainty of 0.2%. The uncertainty in  $C_p$  is a function of the surface pressure and the dynamic pressure. For  $Re = 0.5, 1.0$  and  $1.5$  M, the maximum absolute uncertainty in the measured  $C_p$  was estimated to be  $\pm 0.275, 0.079$  and  $0.031$ , respectively.

### 3.4 Test Results

Selected test data will be discussed in this subsection. Much more data can be found in the original test data reports [2].

Fig. 4 shows a picture of the strake and wing vortices at  $\alpha = 10$  deg illuminated by a laserlight sheet orientated such that it passed through the vortex axes. From the picture it is evident that the strake and wing vortices hardly interact at this angle of attack. Fig. 5 gives a planview of the vortex axes trajectories and core bursting locations observed at the various angles of attack. The interaction between the strake and wing vortices increases with the angle of attack due to the vortices increasing in size and strength. It can be noted that the vortices burst before they cross over.

Fig. 6 shows a picture of the boundary layer flow pattern at  $\alpha = 10$  deg and  $Re = 1.0$  M. The characteristic features of the surface flow pattern are indicated in the sketch. The boundary layer flow pattern on the strake is characterized by outflow markings induced by the strake vortices and clear secondary separation lines. The attachment lines of the primary vortex flow is outboard of the symmetry plane. The secondary separation lines are straight, giving evidence of an approximately conical strake vortex flow. The boundary layer underneath the strake vortex separates at a spanwise position  $y/s \approx 0.70$ , indicating that the boundary layer is laminar. In the case of a turbulent boundary layer, separation would occur more outboard at  $y/s \approx 0.85$  [4]. The topology of the crossflow over the strake is shown in the left sketch of Fig. 7. The free shear layer of the secondary vortex attaches just inboard of the leading edge and induces an inward directed flow on the surface (see insert sketch). This flow separates again at the tertiary separation line. Between the latter line and the secondary separation line a region of accumulated surface oil was visible in the experiment. The pattern showed markings of an outflow that is assumed to be induced by the tertiary vortex. The tertiary separation line was visible from near the apex to the leading edge kink. Downstream of the leading edge kink, this line disappears as the tertiary vortex is supposed to be entrained into the stronger wing vortex.

Downstream of the leading edge kink, at  $\alpha = 10$  deg the shear flow pattern induced by the strake and wing vortices and accompanying secondary separation lines remain individually distinguishable up to the trailing edge. The conjectured topology of the crossflow at  $\alpha = 10$  deg is shown in the right sketch of Fig. 7. It is characterized by a double-branched wing vortex core fed by vorticity from free shear layers that are connected to the wing leading edge and the strake vortex core.

As far as the effect of Reynolds number is concerned, on the strake the pattern changed little when  $Re$  increases from 0.5 to 1.5 M. There were no signs of boundary layer transition from laminar to turbulent. On the wing, the strake vortex secondary separation lines were clearly visible when  $Re = 0.5$  and 1.0 M. From about the 65 % chordwise position, the secondary separation lines at  $Re = 1.0$  M are located outboard those at  $Re = 0.5$  M.

Fig. 8 shows the effect of the angle of attack on the upper surface  $C_p$  at 25% chord for  $Re = 1.0$  M. The  $C_p$ -distribution has been plotted versus the wing lateral coordinate  $y$ , non-dimensionalized by the local wing semispan  $s$ . At  $\alpha = 0$  deg, a small suction peak is induced by the weak strake vortex near the leading edge. Inboard of the suction peak, flow incident to the wing causes a region of positive  $C_p$ . The angle of attack has little effect on the crossflow structure sketched in Fig. 7. The size and circulation of the strake vortex, however, increases with the angle of attack, resulting in a growing suction peak. Outboard of this peak, the pressure curves rise slightly due to the influence of the secondary and tertiary vortices. The level of suction induced by these vortices is about the same as that induced by the primary vortex, confirming that the boundary layer underneath this vortex is laminar. In the case of a turbulent boundary layer, the suction induced by the primary vortex would be larger, while the opposite would be the case for the suction induced by the secondary vortex. There would probably be no tertiary vortex [5].

The effect of the angle of attack on the  $C_p$ -distribution at 75% chord, shown in Fig. 9, can be explained using Fig. 10, which illustrates the effect of the angle of attack on the topology of the crossflow at this station. The latter figure is based on the results of the flow visualization tests. At  $\alpha = 0$  deg, a weak strake vortex suction peak and stronger wing vortex suction peak can be detected in the  $C_p$ -distribution. As the angle of attack is increased to 5 deg, a slight increase can be noted in the strake vortex suction peak and a strong increase of the suction induced by the wing vortices. Outboard of both the strake and the wing vortex suction peak, a suction peak is induced by the accompanying secondary vortex. Up to  $\alpha = 5$  deg, the strake and wing vortices are small and not connected to each other. In the gap between these vortices flow is incident to the wing, causing a small region of positive  $C_p$  at about  $y/s \approx 0.6$ . When the angle of attack is increased further, the strake and wing vortex cores become interconnected. Up to  $\alpha = 12.5$  deg, the suction induced by the strake and wing primary and secondary vortices can be seen to increase. The increase in suction of the wing vortex secondary vortex is only small. This may be due to the transition of the boundary layer underneath the wing vortex from laminar to turbulent which reduces the influence of the secondary vortex. Beyond  $\alpha = 10$  deg, the strake and wing vortices start to coil around each other. The strake vortex moves closer to the wing surface and more outboard, while the wing vortex moves upwards and inboard. The effect of these displacements is noticeable in the  $C_p$ -curves; up

to  $\alpha = 20$  deg the suction peak of the strake vortex moves outboard and increases in size, while the suction peak of the wing vortex moves inboard and reduces rapidly. At  $\alpha = 20$  deg, the wing vortex is overhead the strake vortex and only one suction peak is induced on each wing half. At  $\alpha = 25$  deg, the pressure distribution is affected by the burst of the strake vortex core. As a result, the suction peak not only collapses, but also spreads in the spanwise direction. The latter is caused by the radial expansion of the burst vortex core, through which the circulation previously contained in a narrow core is redistributed over a wider region.

The effect of the Reynolds number on the  $C_p$ -distribution at  $\alpha = 10$  deg was investigated by acquiring data at  $Re$  ranging from 0.5 to 1.5 M. At 25% chord, the effect of  $Re$  on the  $C_p$ -distribution is of the order of the measurement accuracy. At 75% chord, there is a clear effect in the region dominated by the strake vortex (Fig. 11). Due to the transition of the boundary layer underneath the strake vortex from laminar to turbulent, the secondary vortex and its suction have become nil at  $Re = 1.5$  M. This is in accordance with the surface flow pattern where the secondary separation lines have vanished at this  $Re$ . As a result, the primary vortex is located closer to the wing surface, inducing a higher suction than at  $Re = 0.5$  M. On the wing vortex side, transition of the boundary layer results in a smaller and more outboard located secondary vortex. As a consequence, the primary wing vortex is expected to move slightly outboard as well, explaining the slight outboard shift of the wing vortex suction peak that can be noted when  $Re$  is increased from 0.5 to 1.5M.

## 4 Wind Tunnel Wall Corrections

### 4.1 Tunnel Wall Effects

When a wing is tested in a wind tunnel the presence of the tunnel walls will affect the flow around the wing. As a result of blockage, buoyancy and lift interference the flow will be different from that around the wing in free air. The blockage is due to the presence of the wing, its supports and wake, and results in an increase of the dynamic pressure of the flow around the wing. Buoyancy is a result of the axial static-pressure variation in the tunnel test section. The lift interference is associated with the circulation around the wing and affects its angle of attack.

### 4.2 Overview of Wall Correction Methods

In this section an overview is given of the development of wall correction procedures for wings with leading-edge separation. It should be remarked that this is not an overview of all existing wall correction methods for this type of wings.

The first tunnel wall interference correction methods were developed in a time of limited computational capability and are generally referred to as the classical wall correction methods. One such method is the method developed by Garner and Rogers [6]. They model the wing by a lifting line and the wake by trailing vortices which are assumed to remain in the plane of the wing. The latter limits the application of the method to low angles of attack.

Frink [7] uses a free-vortex-sheet (FVS) theory and calculates an improved lift-interference correction for the angle of attack by taking into account the effect of the bending of the trailing vortices into the direction of the freestream.

To account for wake blockage effects, Maskell [8] developed a method based on the measured drag coefficient. This method was improved by Pass [9] for application to models with high blockage ratios. Many blockage correction methods assume that the pressure distribution over the wing is not affected by the wall confinement, or in other words, that the flow transition and separation location remains the same. This so-called principle of invariance under constraint may hold for sharp-edged (double-)delta wings but to lesser extent for large models of complete aircraft configurations. According to Pass [9], the principle of invariance under constraint may be considered valid for configurations with blockage ratios up to 15% (the 76/40-deg double-delta wing considered in this report has a blockage ratio of 10%).

A method for correcting the high- $\alpha$  aerodynamic characteristics of fighter aircraft configurations is the wall-pressure signature method developed by Hackett, et al [10]. This method has the advantage that changes in separation position on the model and wake geometry are automatically accounted for. A minus point is that wall pressures need to be recorded in an extended number of locations not only on the walls of the test section, but often also at locations upstream and downstream of the test section.

To avoid the limitations of the previous procedures, methods are currently developed that are based on CFD solutions for the flow around a model in a wind tunnel. Examples can be found in papers by Thomas and Lan [11], and Verhaagen, et al [12].

The abovementioned methods are discussed in greater detail in the following subsection.

## 4.3 Details of Wall Correction Methods

### 4.3.1 Method of Garner and Rogers

The method is based on linear potential flow theory and uses images to predict wall interference. The wing is modeled by a lifting line and its wake by trailing vortices which are assumed to remain in the plane of the wing.

The blockage of the flow in the tunnel due to the presence of the wing and its wake is assumed to increase the velocity around the model by an increment  $\Delta U_B$ . The blockage factor  $\epsilon_B$ , being the sum of the solid, wake and streamwise-velocity interference blockage factors  $\epsilon_s$ ,  $\epsilon_w$  and  $\epsilon_v$ , can then be written as

$$\epsilon_B = \epsilon_s + \epsilon_w + \epsilon_v = \frac{\Delta U_B}{U} \quad (1)$$

For a "small" three-dimensional wing ( wing span less than 0.5 tunnel width ) in a rectangular test section the solid blockage factor is given by ([6], equation 5.29)

$$\epsilon_s = \frac{TV}{C^{3/2}\beta^3} \left[ 1 + 1.2\beta\frac{t}{c} \right], \quad (2)$$

where

$$T = 0.65\sqrt{\frac{B}{H}} \quad (3)$$

and

- $B$  = tunnel width
- $H$  = tunnel height
- $V$  = volume of the wing
- $C$  = tunnel cross-sectional area
- $\beta = \sqrt{1 - M^2}$
- $t$  = model thickness
- $c$  = root chord length

The wake blockage factor is given by ([6], equation 5.53)

$$\epsilon_w = \frac{1}{4} \frac{S C_D}{C \beta^2} \quad (4)$$

If the wing is displaced vertically off the center of the tunnel, there exist both stream-wise and upward interference velocities. The streamwise velocity perturbation creates another blockage effect, called the stream-velocity interference factor. This is expressed as ([6], equation 3.27)

$$\epsilon_v = \delta\left(\frac{d}{H}, \frac{B}{H}\right) \frac{S.C_L}{\beta B H}, \quad (5)$$

where  $d$  denotes the distance from the wing to the tunnel floor.

In incompressible flow the blockage factor is applied directly to the dynamic pressure by

$$q = q_m(1 + \epsilon_B)^2 \approx q_m(1 + 2\epsilon_B), \quad (6)$$

where  $q_m$  is the measured dynamic pressure.

The lift effect is due to the lift interference and streamline curvature effects. These effects induce an upwash normal to the freestream which increases the effective  $\alpha$  of the wing. The correction in velocity direction is averaged over the wing so that it can be applied to the angle of attack  $\alpha$ .

Representing the wing by a semi-infinite vortex pair and using the image method to satisfy the boundary condition on the walls, the following correction is derived ([6], equation 3.182)

$$\Delta\alpha = \frac{SC_L}{C} \left[ \delta_0 + \frac{c - x_p}{\beta H} \delta_1 \right], \quad (7)$$

where

$\delta_0$  = the averaged upwash interference parameter at the lifting line ( $0.25 \bar{c}$ )

$\delta_1$  = the upwash interference due to streamline curvature

$x_p$  = center of pressure

The parameter  $\delta_0$  ([6], equation 1.34) is a function of the wing-to-tunnel span ratio  $R_b$  and the tunnel cross-section ratio  $R_t$ . The lifting line model assumes the trailing vortices to be in the plane of the wing. This implies that the corrections are in fact applicable for small angles of attack only.

Karou [13] applied the above corrections for blockage and lift effects to the balance data of a 76-deg delta wing tested in a tunnel with different  $R_t$  ratios at TUDelft. The data were recorded at angles of attack up to 22.5 deg. That is far below the angle at which vortex burst occurs over the wing ( $\approx 35$  deg). The corrected data for the three values of  $R_t$  collapsed to a single line which was shown to be in very good agreement with other experimental data.

#### 4.3.2 Method of Frink

Frink [7] extended the lifting-line interference correction using a free-vortex-sheet (FVS) theory. By using the doublet distribution from the tunnel walls, which contains the pressure distribution induced by the delta wing, he computed upflow variations at the wing such as the streamline curvature and aerodynamic twist. Fig. 12 shows the effect of  $R_b$  on the streamline curvature predicted at the rootchord of a 65-deg swept delta wing for  $\alpha = 15$  and 30 deg. The upflow angle can be seen to increase with  $R_b$  and

along the rootchord with the angle of attack. Fig. 13 shows a similar tendency for the spanwise variation of the wall-induced aerodynamic twist. Using his FVS solution he further showed that the averaged upflow parameter  $\delta_0$  not only is a function of  $R_b$  and  $R_t$ , such as is assumed in the lifting-line theory of reference [6], but also depends on the angle of attack. In the lifting-line theory the trailing vortices are assumed to remain in the plane of the wing, limiting its application to angles of attack up to approximately 20 deg. Frink showed that if the bending of the wake vortices into the direction of the free stream is taken into account,  $\delta_0$  becomes a function of  $C_N$  and  $\cos\alpha$ , rather than  $C_L$ , and can be written as

$$\delta_0 = \left(\frac{\Delta\alpha}{C_N}\right)\left(\frac{4R_t}{R_b^2 \tan\Lambda}\right) \cos^{p-1}\alpha \quad (8)$$

where the cosine power  $p$  will be near 1 if the angle of attack is small, and near 2 at larger angles. His solution does not provide a correction for blockage or streamline curvature. Frink computed corrections for a 65-deg delta wing tested in the NASA LaRC LTPT (Low-Turbulence Pressure Tunnel) and for a large ( $R_b = 0.584$ ) semispan 76-deg delta wing tested in the TUDelft LTT (Low-Turbulence Tunnel) [12]. The corrections to the 65-deg delta wing flowfield were shown to be good for  $R_b$  values up to 0.5 and angles of attack up to 30 deg. For the 76-deg delta wing the effect of the averaged upflow angle appeared to be corrected satisfactory. The effects of streamline curvature were noted to be large, but no values were given.

#### 4.3.3 Wake Blockage Correction Method

The correction method of Pass [9] was developed for semispan wings which are tested in small subsonic wind tunnels. The method is based on a model of bluff body flow proposed by Maskell [8]. Assuming an axi-symmetric wake, he derives the following relation for the change in dynamic pressure:

$$\frac{\Delta q}{q} = \frac{1}{k^2 - 1} \cdot C_{Ds} \cdot \frac{S}{C} \quad (9)$$

where  $k$  is the base pressure parameter and  $C_{Ds}$  the separation drag coefficient. He further assumed that the separation location of the body and wake flow is not affected by the wall confinement. His model is considered valid for (full) configurations with blockage ratios of up to 10%. The  $C_{Ds}$  can be determined from the  $C_L^2$  vs  $C_D$  curve (fig. 14). This procedure works well for straight wings, but becomes problematic if the curve is non-linear such as in the case of (double-)delta wings. To make Maskell's correction procedure applicable to a wider range of semispan geometries, Pass conducted an extensive series of experimental tests on straight, tapered and delta wing configurations. Based on the test results an empirical alteration to Maskell's expression (equation 9) was developed specifically for semispan models with a blockage ratios up to 29%.



#### 4.3.4 Pressure Signature Method

The wall pressure signature method of Hackett, et al, [10] makes use of the static pressure distribution measured along the tunnel walls. The so-called "interference" flowfield at the location of the wing is computed by using a (vortex or doublet) singularity distribution with a strength determined by the measured wall pressure distribution. Hackett, et al, suggest to measure pressures along the centerlines of the tunnel floor, ceiling and side walls. The method has the advantage that changes in separation position on the model and wake geometry are automatically accounted for. A minus point is that wall pressures need to be recorded in an extended number of locations on the walls of the test section. To verify the asymptotic behavior of the pressure distribution along the walls, it is often necessary to also take pressures at locations upstream and far downstream of the test section. The wall pressure signature method is reported to be applicable to aircraft geometries of blockage ratios up to 20% [9]. Care should be taken when applying this procedure to configurations with extended flow separation, such as present over delta wings at large angle of attack or sideslip. To determine the local singularities in the wall pressure distribution induced by the wing, its support and wake, it may be necessary to take pressures not only at the centerline of the tunnel walls but also at other wall locations.

#### 4.3.5 Numerical Simulations

Thomas and Lan [11] used a thin-layer Navier Stokes solver to simulate the flow about a 76-deg delta wing in the BART at NASA LaRC. The tunnel wall pressures were not measured as in the former method, but were computed and used as the boundary condition for an Euler solution of the wind tunnel flow without the presence of the delta wing (Fig. 16). The computed interference flowfield was used to estimate the blockage and upwash effects needed to correct the wing forces to free air conditions. The corrected  $C_L - \alpha$  curve was shown to agree well with the balance data obtained in the larger 7-ft by 10-ft (2.1-m by 3.0-m) wind tunnel at NASA LaRC.

Verhaagen, et al, [12] compute the flow over a large-size semispan 76-deg delta wing in the LTT of TUDelft using an Euler solver. The effect of  $R_b$  on the leading-edge vortex flow and the aerodynamic forces was determined from solutions developed for the flow around the wing in tunnels of different cross-sectional geometries and for the wing in free air. The solutions showed that an increase of  $R_b$  results into an increase of the magnitude of the velocities and pressures in the vortex core. This is accompanied with an increase of the vortex strength and the forces acting on the wing.

### 4.4 Discussion

In the next section the tunnel wall corrections will be applied to the test data of the 76/40-deg double-delta wing. For these corrections the method developed by Garner and Rogers [6] was selected. Karou [13] has shown that this method gives good results for a 76-deg delta wing up to  $\alpha = 22.5$  deg angle of attack. The improved correction for the averaged upflow parameter  $\delta_0$  suggested by Frink [7] will not be applied, because in order to be able to determine this parameter a FVS solution is needed for the flowfield over the double-delta wing. Such a solution is not provided in reference [7]. The wake blockage



correction proposed by Maskell [8] will not be applied either, because this correction can be determined only if the  $C_L^2$  vs  $C_D$  curve is linear over a large range of angles of attack. Data computed in reference [1] indicate that this is not the case for a 76/40-deg double-delta wing (Fig. 15).

## 5 Corrections applied to BART Test Data

### 5.1 Blockage Effect

The ratio between the wing area and the cross-sectional area of the tunnel test section  $S/C$  is called the blockage ratio. For the present wing and tunnel,  $S = 0.0711 \text{ m}^2$  and  $C = 0.724 \text{ m}^2$ , so that

$$S/C = 0.0982$$

Using the following data for the wing and tunnel,

$$B = 1.02 \text{ m}$$

$$H = 0.71 \text{ m}$$

$$V = 2.015 \cdot 10^{-3} \text{ m}^3^*$$

$$\beta \approx 1$$

$$t = 9.53 \text{ mm}$$

$$c = 0.406 \text{ m}$$

with equation 2 it can be calculated that

$$\epsilon_s = 0.00262$$

The solid blockage factor is independent of the angle of attack. This factor will also be affected by the post and sting which supports the wing in BART. In addition, the pressure tubes behind the wing (Fig. 3) may have some influence. Since the dimensions of these parts were not measured during the tests, the effect of these parts is not taken into account here for the solid blockage factor.

To compute the wake blockage factor with equation 4, a value is needed for the drag coefficient  $C_D$ . Because no balance measurements were conducted on the present wing, the force coefficients are used which were computed for the same wing by Kern [1]. He solved the flow over the wing in free air. An estimation is then needed of the effect of tunnel walls on  $C_L$  (and  $C_D$ ). This has been obtained from data published by Washburn [14]. He compares balance data obtained for a 76-deg delta wing in the BART with data recorded with the same wing in the 7-ft by 10-ft tunnel at NASA LaRC. His data show an increase in  $C_L$  vs  $\alpha$  due to tunnel wall interference. Another effect is that of the fairing at the lower surface of the wing. Washburn's data showed that the fairing only influences the effective wing camber but not the slope of the  $C_L$  vs  $\alpha$  curve. The negative camber effect decreased the  $C_L$  by an average value of 0.04 throughout the angle of attack range. One of the differences between the flow over a 76-deg delta wing and that over a 76/40-deg double-delta wing is, e.g., that bursting occurs over the double-delta wing at already low angles of attack (Fig. 5). The burst location may be affected by the fairing on the lower surface of the wing. Guglieri and Quagliotti [15] studied the effect of a fairing at the lower surface of a 65-deg delta wing on the vortex breakdown location. At  $\alpha = 20$  deg, the presence of the fairing resulted into a 20% chord more upstream location of the vortex burst.

In the following computations the effect of the tunnel wall interference and the fairing

---

\* $V$  = the estimated volume of the wing ( $.518 \cdot 10^{-3} \text{ m}^3$ ) plus the estimated volume of the fairing ( $1.497 \cdot 10^{-3} \text{ m}^3$ )

on the  $C_L$  (and  $C_D$ ) of the 76/40-deg double-delta wing is assumed to be the same as that measured by Washburn for the 76-deg delta wing in BART. The author is aware that this assumption is debatable and should be verified in future tests, if possible. The assumptions are made here since, to the author's knowledge, no other data is available to quantify these effects. Table 1 gives the values of  $C_D^1$  computed in reference [1] for the wing in free air, of the estimated  $C_D$  for the wing in BART, and of  $\epsilon_w$  for three angles of attack.

$\alpha$ (deg)	$C_D^1$ ref. [1]	$C_D$	$\epsilon_w$ eq. (4)
10	0.09	0.09	0.00221
15	0.21	0.22	0.00540
20	0.36	0.38	0.00993

Table 1.

To compute the streamwise-velocity interference factor with equation 5, the distance from the wing to the tunnel floor  $d$  should be known. This distance, unfortunately, was not measured during the testings at BART. Washburn [14] used the same support for a 76-deg delta wing and found that ([14], table B.1)

$$\frac{d}{H} = \frac{9.7'' + 10.6'' \sin(19.8^\circ + \alpha)}{28''} \quad (10)$$

With this ratio

$$\delta\left(\frac{d}{H}, \frac{B}{H}\right) = \epsilon_v \left(\frac{\beta B H}{S C_L}\right) \quad (11)$$

can be determined using Fig. 3.3 of [6].

The computed values of  $C_L^1$ ,  $C_L$ ,  $\frac{d}{H}$ ,  $\delta$  and  $\epsilon_v$  are given in table 2.  $C_L$  represents the estimated lift coefficient of the wing in BART.

$\alpha$ (deg)	$C_L^1$ ref. [1]	$C_L$	$\frac{d}{H}$ eq. (10)	$\delta$ eq. (11)	$\epsilon_v$ eq. (5)
10	0.34	0.35	0.535	0.018	0.00062
15	0.66	0.69	0.562	0.032	0.00216
20	0.86	0.90	0.589	0.046	0.00407

Table 2.

Summating the solid, wake and stream-interference factors yields the blockage factor  $\epsilon_B$ . Substituting this factor into equation 6 gives the blockage correction for the dynamic pressure. Results are given in table 3.

$\alpha$ (deg)	$\epsilon_B$ eq. (1)	$\frac{q}{q_m}$ eq. (6)
10	0.00545	1.0190
15	0.01018	1.0204
20	0.01602	1.0320

Table 3.

Fig. 17 shows the variation of the different blockage factors with the angle of attack. The solid blockage is independent of  $\alpha$ . It should be reminded that its value may be larger than calculated here due to the effect of the support and the pressure tubes. Both the wake and streamwise-velocity blockage can be seen to both increase with the angle of attack. The contribution of the wake blockage is the largest.

## 5.2 Lift Effect

The correction for the average velocity direction is computed using equation 7. According to reference [6], Fig. 3.2, for the present tunnel  $\delta_0 = 0.116$  and  $\delta_1 = 0.232$ . No correction was applied for the off-center location of the wing. Fig. 3.3 of reference [6] suggests this correction to be small. The center of pressure  $x_p$  has been calculated using the computed force and moment data of again reference [1]. According to Washburn and Visser [16], the post support induced an upwash on the order of 2 deg. Table 4 gives the value of  $x_p$ , and the increase in effective angle of attack  $\Delta\alpha$  due to the upwash computed with equation 7 and the upwash induced by the post support.

$\alpha$ (deg)	$x_p$ (%c)	$\Delta\alpha$ (deg)
7.5	0.453	2.21
10	0.550	2.35
12.5	0.589	2.56
15	0.617	2.65
17.5	0.620	2.78
20	0.621	2.84

Table 4.

The increase in effective  $\alpha$  leads to a larger vortex strength and lower upper-surface  $C_p$ . The  $C_p$ -distributions were corrected for  $\Delta\alpha$  by linear interpolation between the data recorded at  $\alpha + \Delta\alpha - 2.5$  deg and  $\alpha + \Delta\alpha$  deg.

## 5.3 Wall Corrections applied to $C_p$ -Distributions

Figs. 18 and 19 show the effect of both the blockage and the lift effect correction on the  $C_p$ -distribution at 25 and 75% chord for  $\alpha = 10$  and 20 deg, respectively. Applying the wall corrections, especially the lift correction, result into a much lower level of  $C_p$  and,

as shown in Fig. 20 for  $\alpha = 10$ , reduces the deficiency between the laminar solution and the experiment. Differences remain between the predicted and measured  $C_p$ -distributions, which can not fully be attributed to the small difference in Reynolds number used for the solution and the experiment. The differences are supposed to be due to inaccuracies in the wall interference correction procedure and the numerical modeling. It should further be reminded, that the corrections rely on wall effects measured by Washburn and Visser ([14] and [16]) on a 76-deg delta wing, and not a 76/40-deg double-delta wing, tested in the BART. It would have been interesting to compare the corrected data presented in Fig. 20 with the data measured on the 76/40-deg double-delta wing in the 7-ft by 10-ft tunnel at NASA LaRC. Unfortunately, the author of this report was not permitted to use the data measured in this tunnel.

## 6 Tunnel Wall Effects on Vortex Breakdown; A Literature Survey

The location of the vortex core breakdown over a delta wing is a function of the angle of attack, sideslip, roll angle, and leading-edge sweep. It is also affected by the geometry, beveling and thickness of the wing. Experimental data can be found in references [17] - [21], and others.

In this section the influence of the effect of tunnel walls on the vortex core breakdown location over a delta wing is discussed.

Weinberg [22] computed this effect using a method of vortex images. Inside the tunnel both leading-edge vortices and an additional pair of vortices representing the wing's bound vorticity were modeled. Along the wing an upwash distribution was calculated that was small near the apex and increased towards the trailing edge, indicating that an effectively cambered wing is created under the influence of the tunnel walls. Using a nonlinear vortex lattice method, he computed the distribution of  $C_p$  along the axis of the leading-edge vortex over a flat and a cambered delta wing. Above the flat wing  $C_p$  reached its lowest value at about 30% chord, while above the cambered wing the minimum  $C_p$  was located more downstream at about 50% chord due to the continuously increasing local  $\alpha$  along the wing chord. Since breakdown is caused by an adverse pressure gradient, the vortices above the cambered wing can be expected to burst downstream of the breakdown location of the flat wing. Weinberg remarks that this conclusion is opposite to the intuition that wall effects tend to increase the effective  $\alpha$ . Such an increase would result in correcting the breakdown location towards the trailing edge, whereas the appropriate correction, when taking the effective camber into account, is towards the apex. Weinberg investigated the wall effect in a water tunnel experiment using two sets of three delta wings which had a leading-edge sweep angle of 60 and 70 deg. The three wings in each set increased linearly in size, while keeping a similar wing geometry. For the 70-deg wings, the breakdown location was observed to move continuously downstream as the wing increases in size. This is in accordance with the predicted trend. The breakdown location for the 60-deg wings did not follow the predicted trend as well as the wings with the higher sweepback. Weinberg concluded that his method of images is valid for small aspect ratio wings only.

Pelletier and Nelson [23] investigated the effect of tunnel walls on three 70-deg swept delta wings that also increased linearly in size and were geometrically similar. The tests were conducted in a water tunnel at  $Re = 35,000$  and angles of attack up to 45 deg. The results showed that for a given  $\alpha$  the vortex breakdown location moved upstream with increasing wing size, and hence increasing blockage. This does not agree with the abovementioned test results of Weinberg and his theory of effective camber. Pelletier and Nelson modeled the tunnel walls using four image vortices (two for each leading-edge vortex). The image vortices induce an upwash which increases with wing size and leads to a larger effective  $\alpha$ . According to their theory, the location of the vortex breakdown on a larger wing should thus be upstream of that on a smaller wing because the wing experiences a larger  $\alpha$ . This is in accordance with the observations in their water tunnel experiment. They further showed that the vortex breakdown location of the three wings

tend to match when the change in velocity at the model due to blockage is taken into account.

## 7 Conclusions and Recommendations

Surface-pressure data of a 76/40-deg double-delta wing tested in the BART at NASA LaRC were corrected for tunnel wall interference effects using a flowfield correction method. The correction is shown to improve the correlation between the computed and measured  $C_p$ -data. Deficiencies between the computed and measured  $C_p$  remain and may be due to inaccuracies in the wall correction procedure and the numerical modeling.

To improve the accuracy of experimental dataset, it is recommended to include balance measurements in future wind tunnel tests and to pay attention to the effect of the wing support and the fairing at the lower surface of the wing on the balance data. It is further recommended to include the tunnel walls and support configuration in the numerical model.

Surprisingly few experimental data is available on the effect of tunnel walls on the location of vortex core breakdown. Published data of experiments in water tunnels show contradictory results. To obtain a better insight and more unique information on the effect of the tunnel walls on vortex breakdown, it is recommended to study this effect by conducting tests in water and wind tunnels with (double-)delta wings of different size. NAWC has an excellent wind tunnel at PAX River to carry out this type of testings. The testings in a water tunnel could be performed using the facility of the Naval Post Graduate School at Monterey. Besides these experiments, solutions of the Navier-Stokes equations could also help obtain a better understanding of this wall effect.

## 8 Acknowledgements

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## 9 References

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## 10 Figures

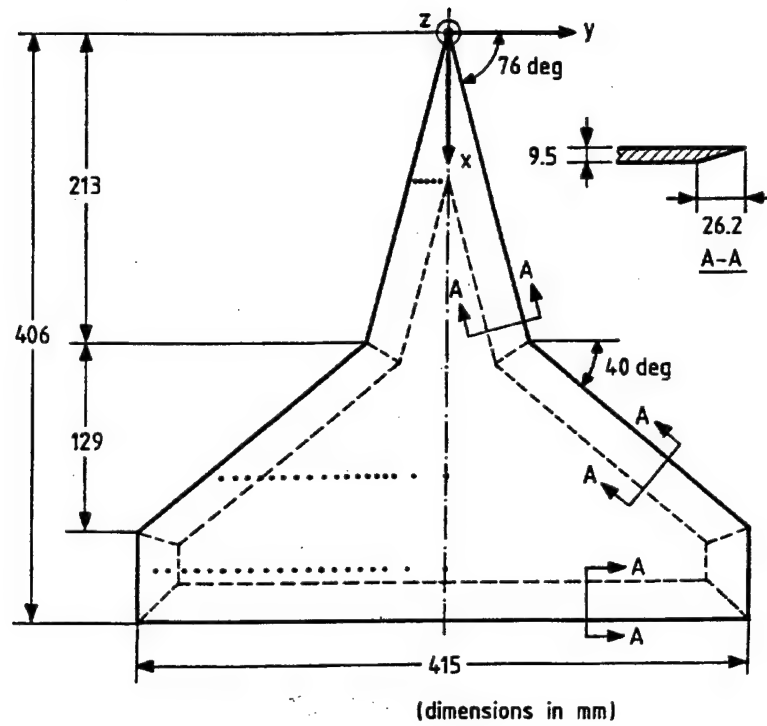


Figure 1: Double-delta wing geometry

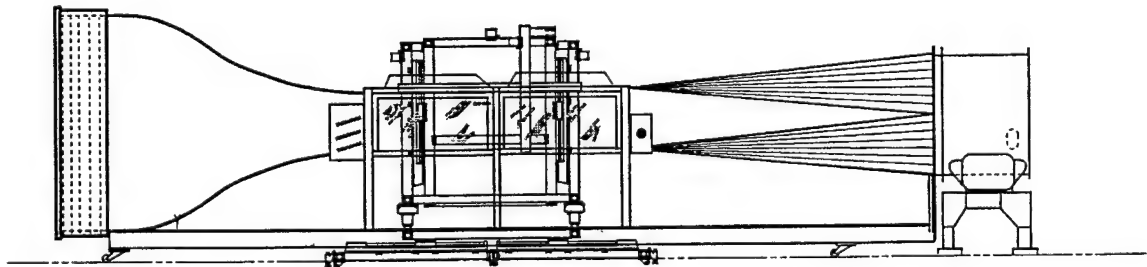


Figure 2: BART tunnel

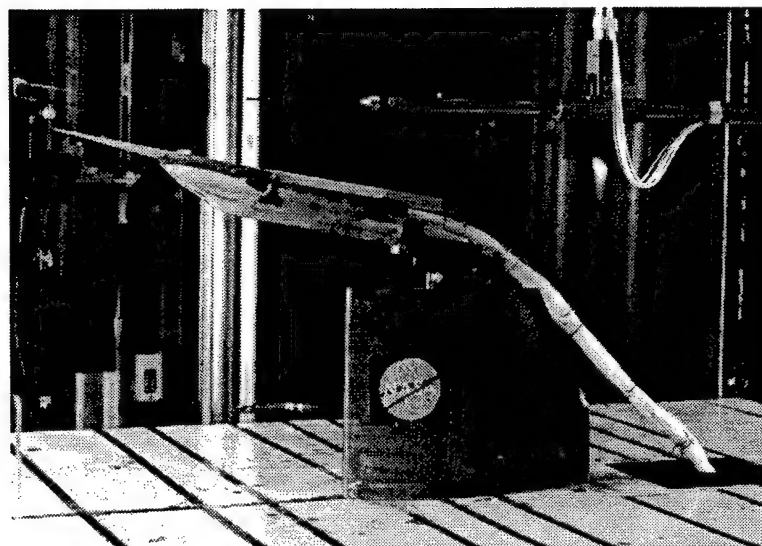
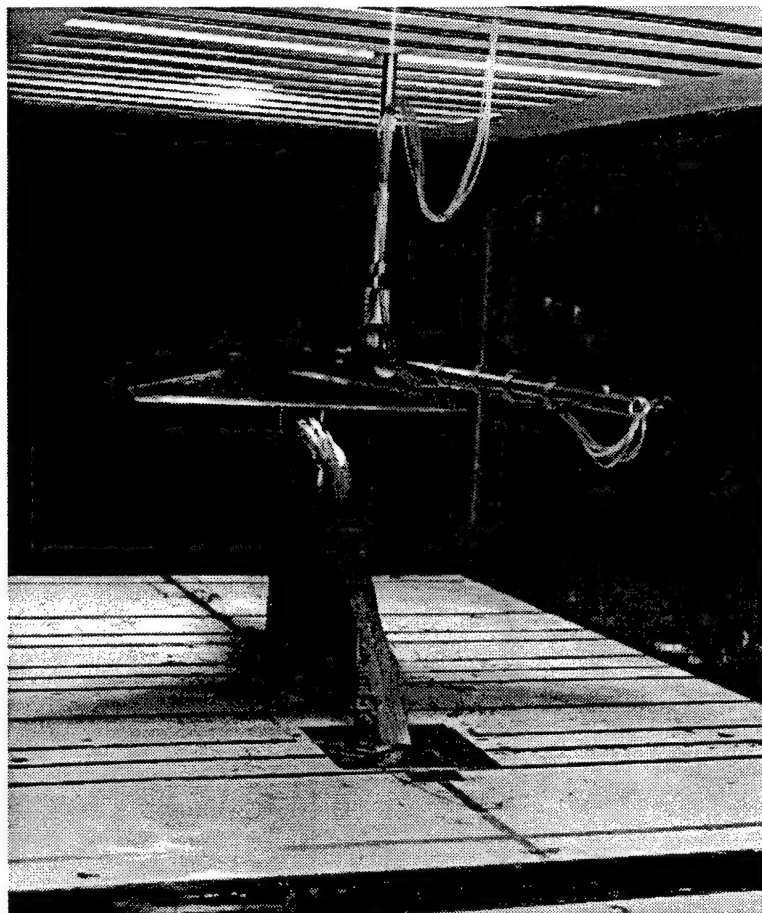


Figure 3: Wing in BART tunnel

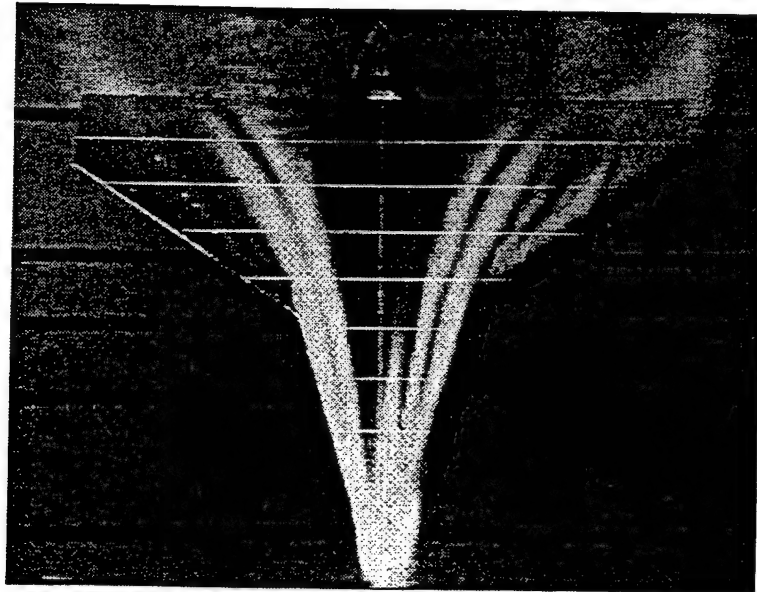


Figure 4: Vortices illuminated by laserlight sheet;  $\alpha = 10$  deg

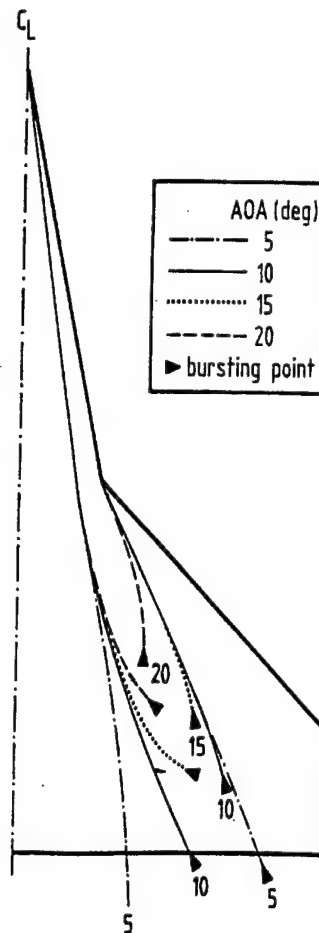


Figure 5: Effect of  $\alpha$  on vortex axis trajectory and core burst location

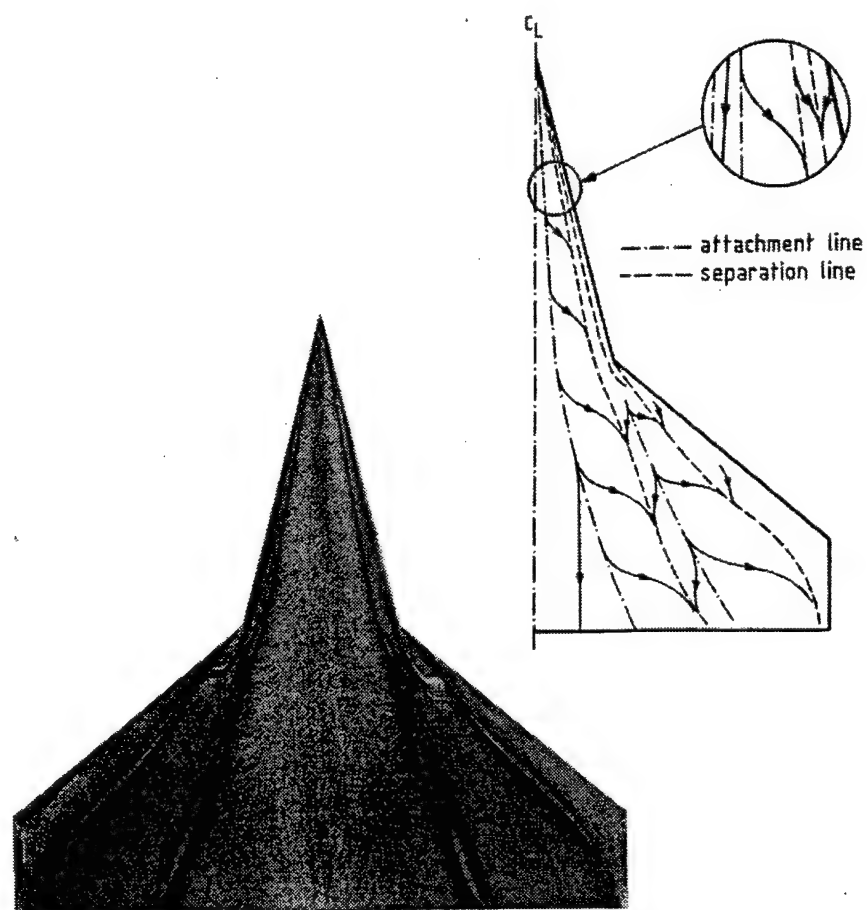


Figure 6: Upper surface flow pattern;  $\alpha = 10$  deg,  $Re = 1.0$  M

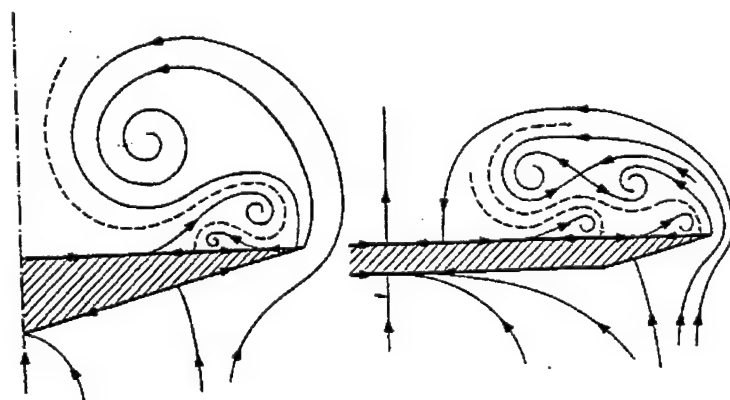


Figure 7: Topology of crossflow over strake (left) and wing (right sketch)

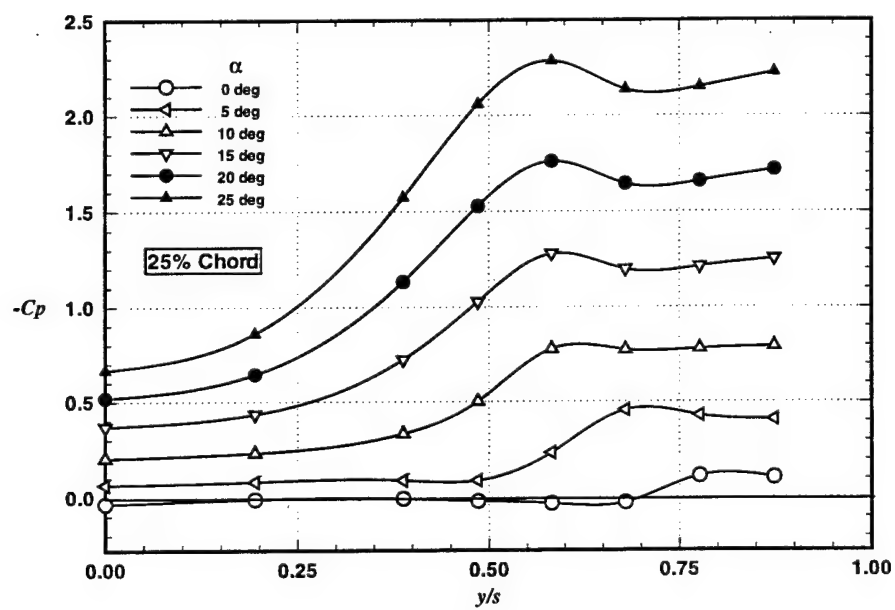
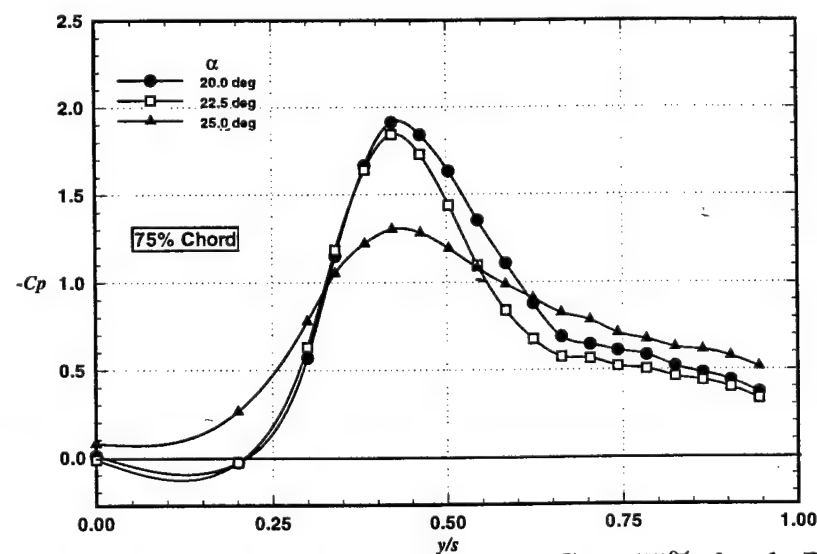
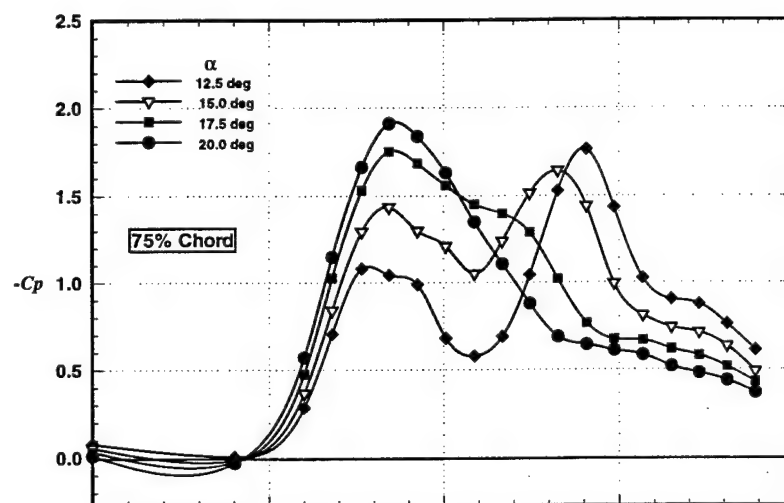
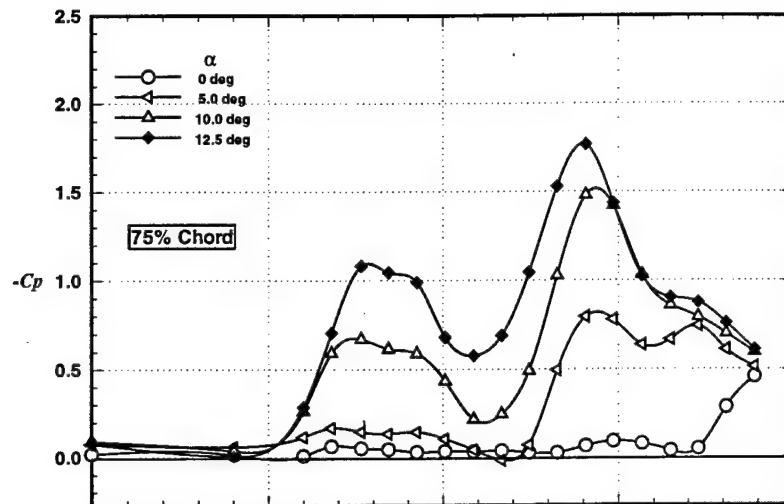


Figure 8: Effect of  $\alpha$  on upper-surface  $C_p$  at 25% chord;  $Re = 1.0 \text{ M}$





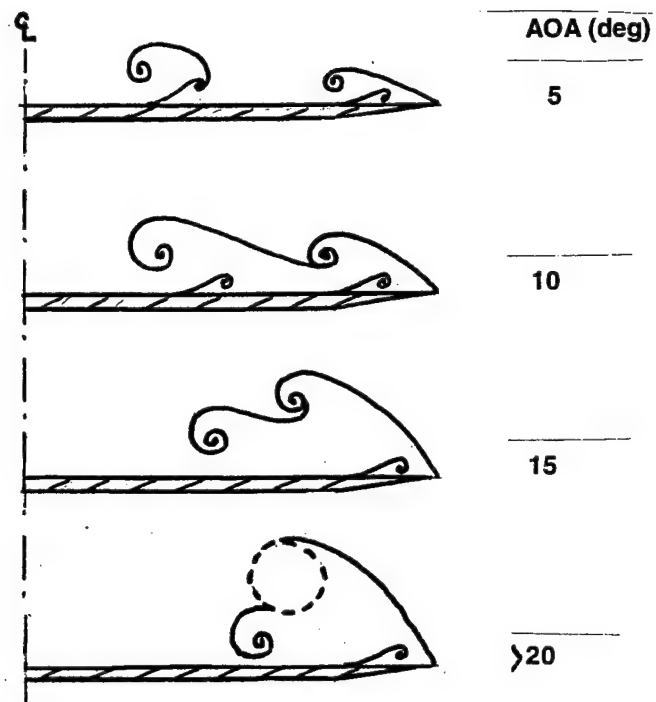


Figure 10: Effect of  $\alpha$  on crossflow topology at 75% chord

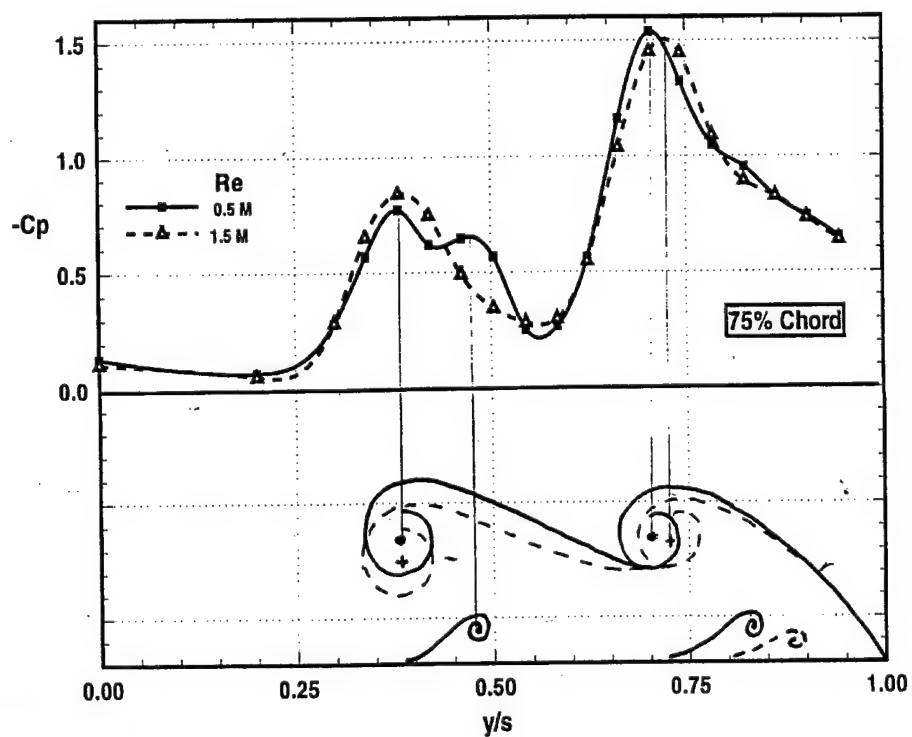


Figure 11: Effect of  $Re$  on upper-surface  $C_p$  at 75% chord;  $\alpha = 10$  deg

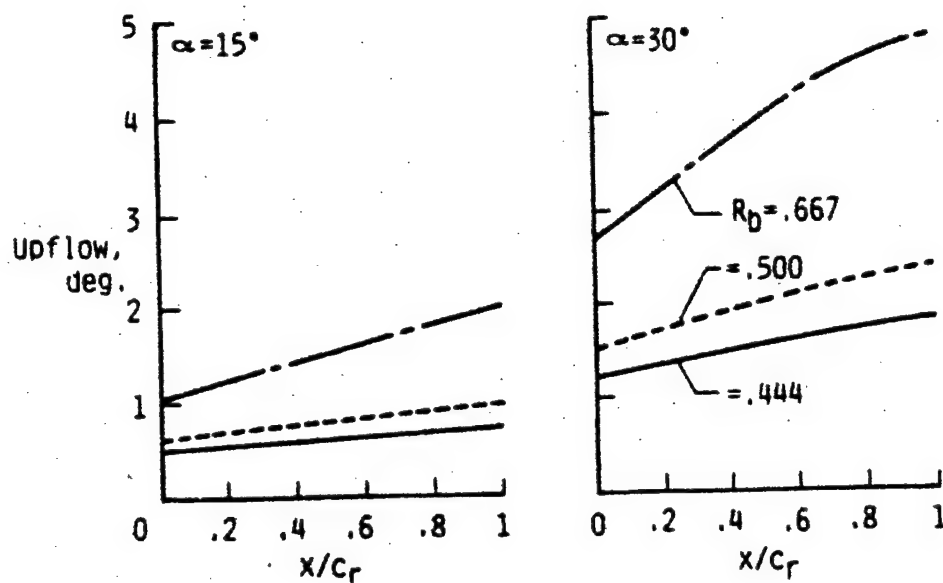


Figure 12: Computed effect of  $R_b$  on streamline curvature along root chord; 65 deg delta wing,  $R_t = 2.5$  (Frink [7])

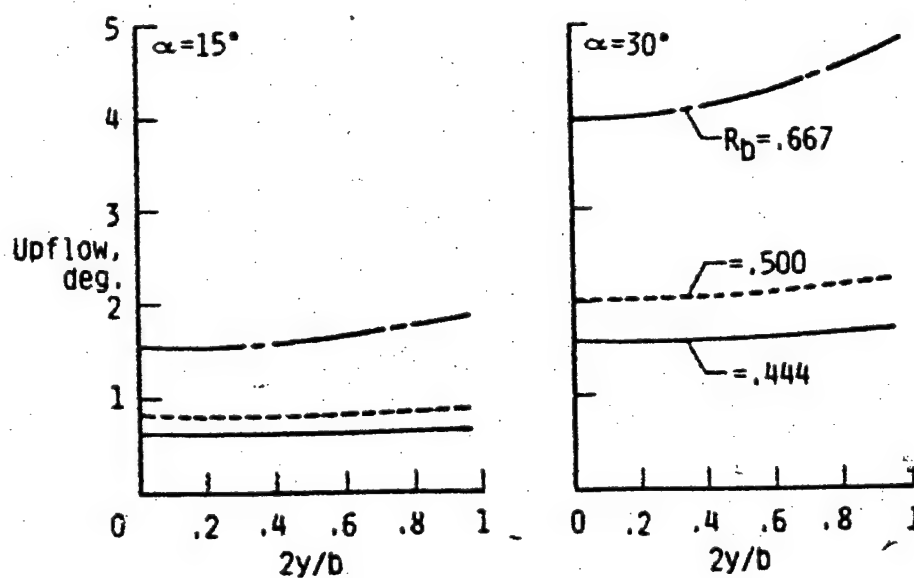


Figure 13: Computed effect of  $R_b$  on aerodynamic twist at mid chord station; 65 deg delta wing,  $R_t = 2.5$  (Frink [7])

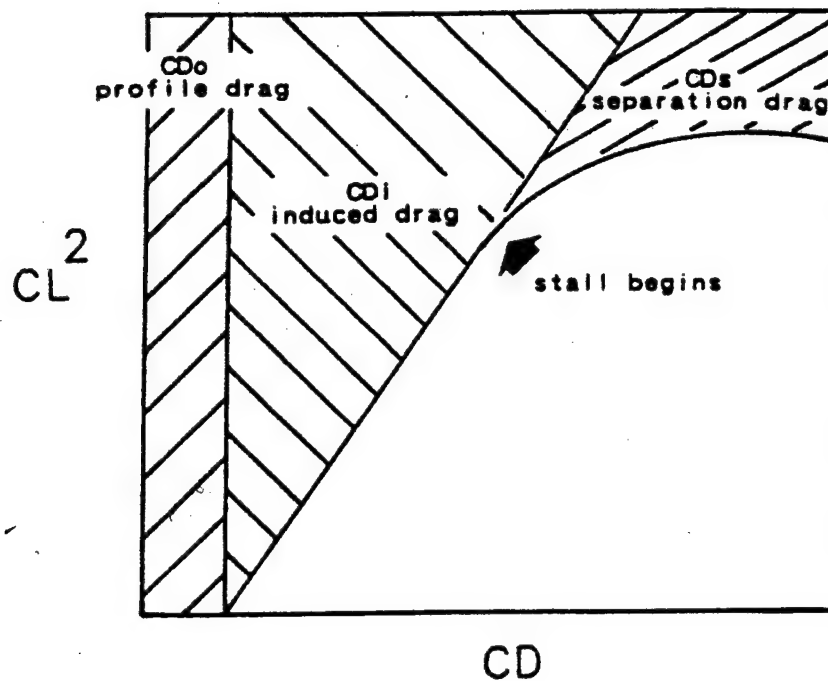


Figure 14: Method of separating drag components (Maskell [8])

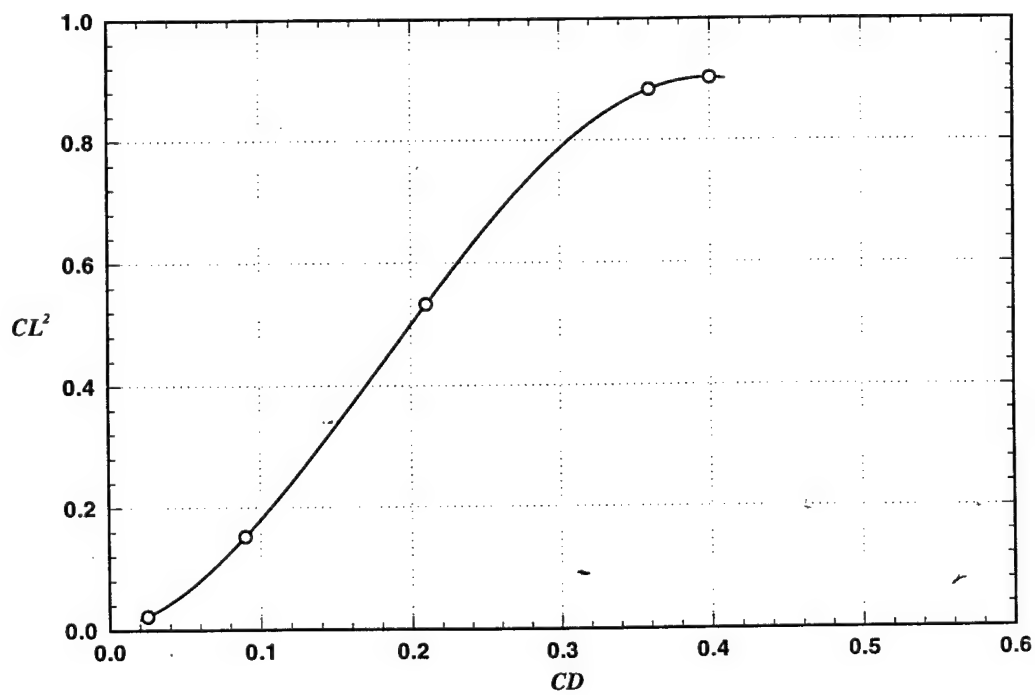


Figure 15: Computed  $CL^2$  vs  $CD$  (Kern [1])

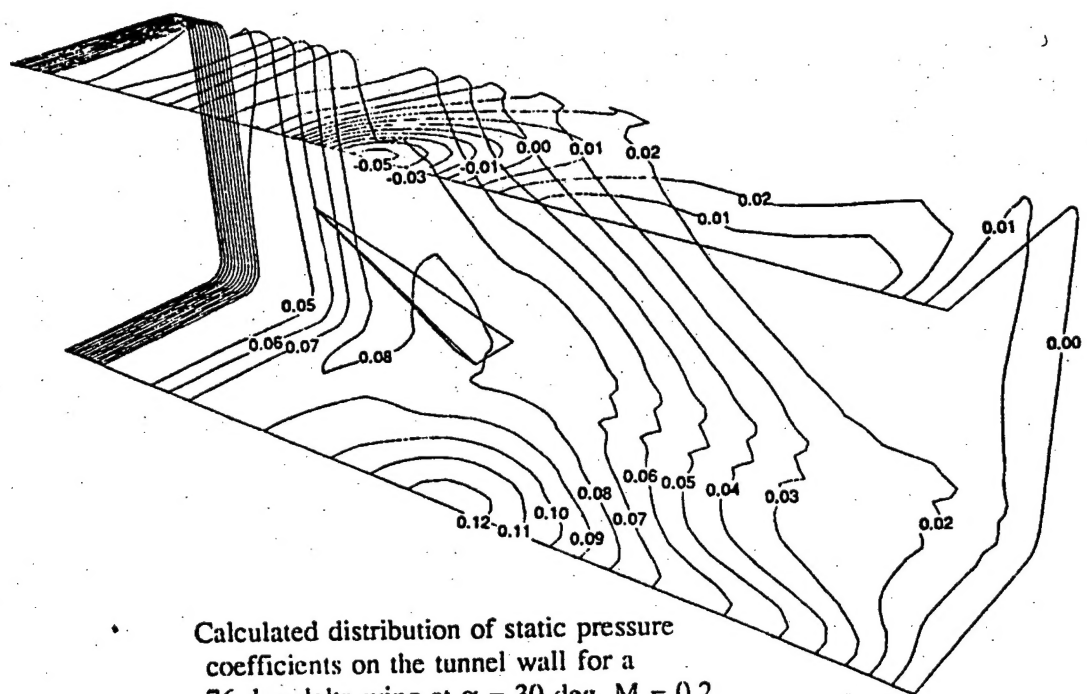


Figure 16: Computed  $C_p$ -distribution induced on walls of BART by a 76-deg delta wing (Thomas and Lan [11])

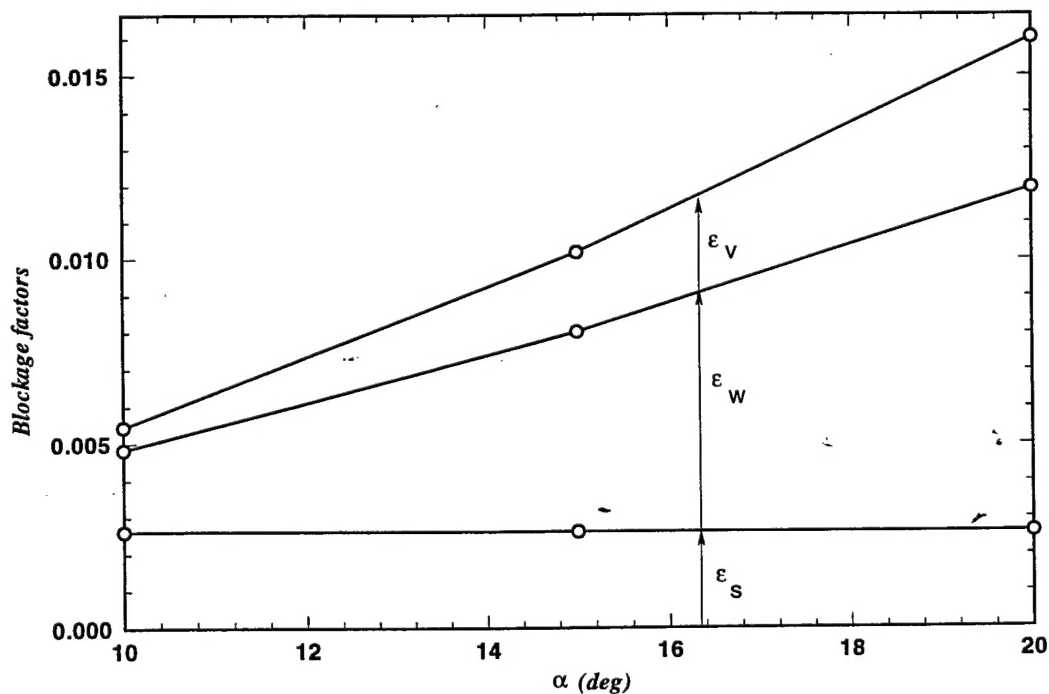


Figure 17: Effect of  $\alpha$  on blockage correction factors

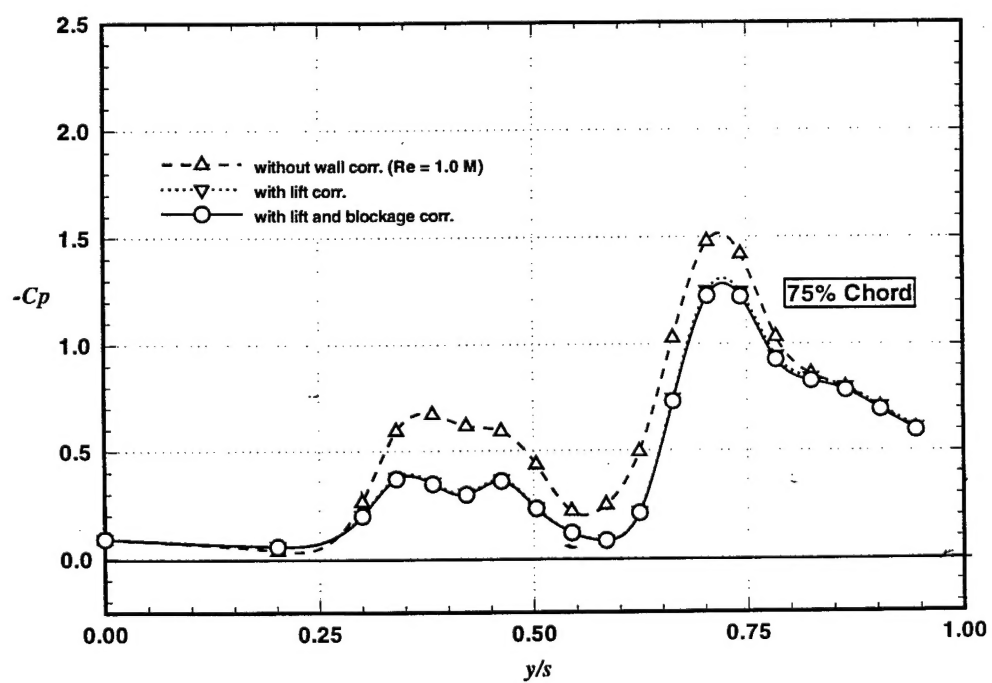
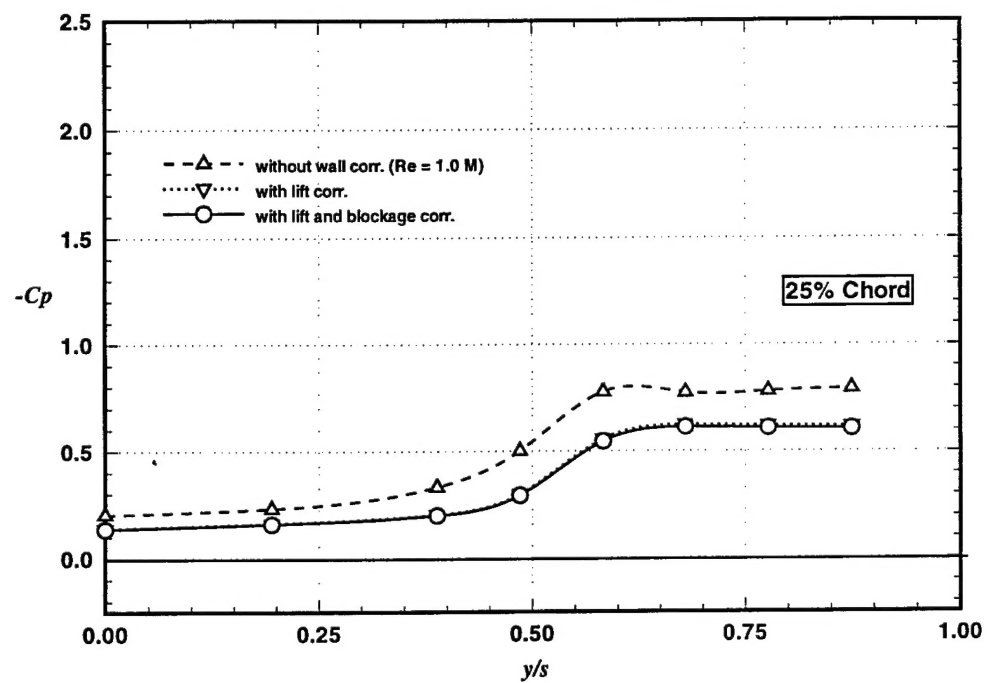


Figure 18: Effect of lift and blockage corrections;  $\alpha = 10$  deg,  $Re = 1.0$  M

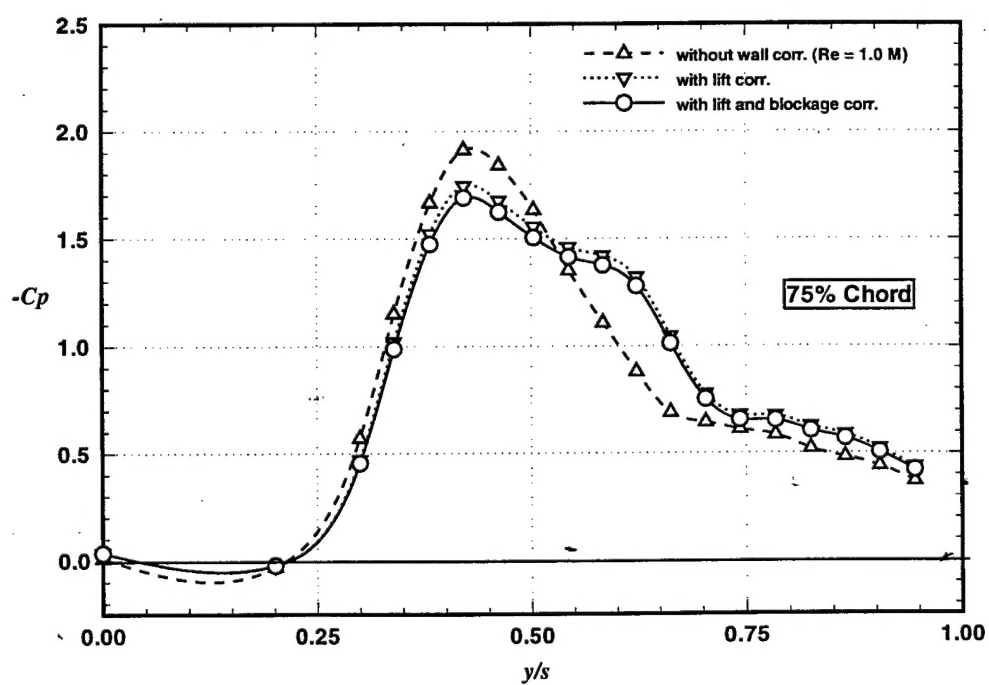
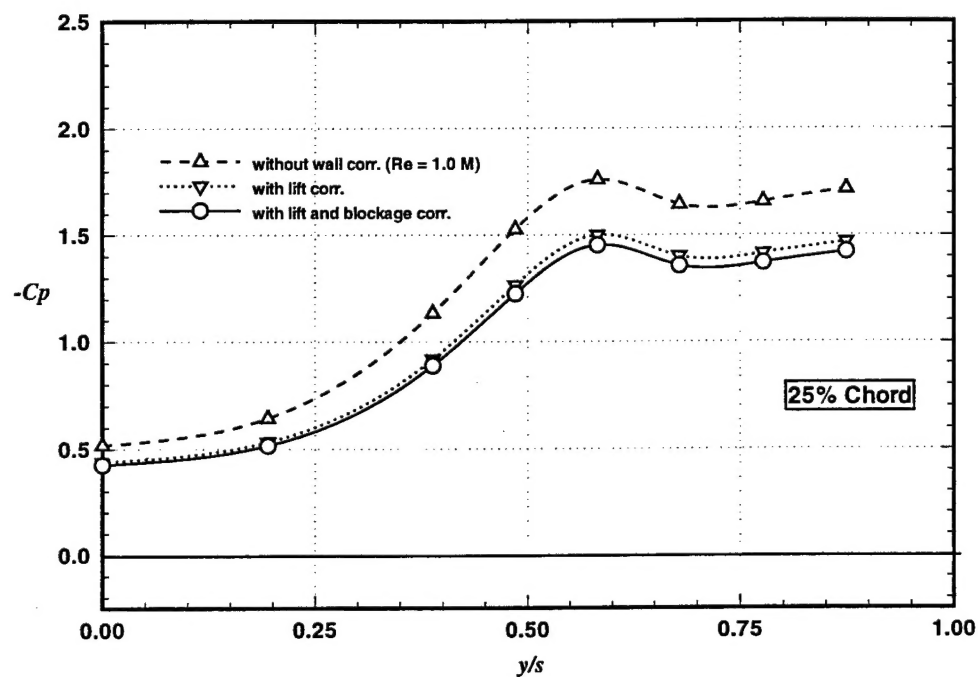


Figure 19: Effect of lift and blockage corrections;  $\alpha = 20^\circ$ ,  $Re = 1.0 \text{ M}$

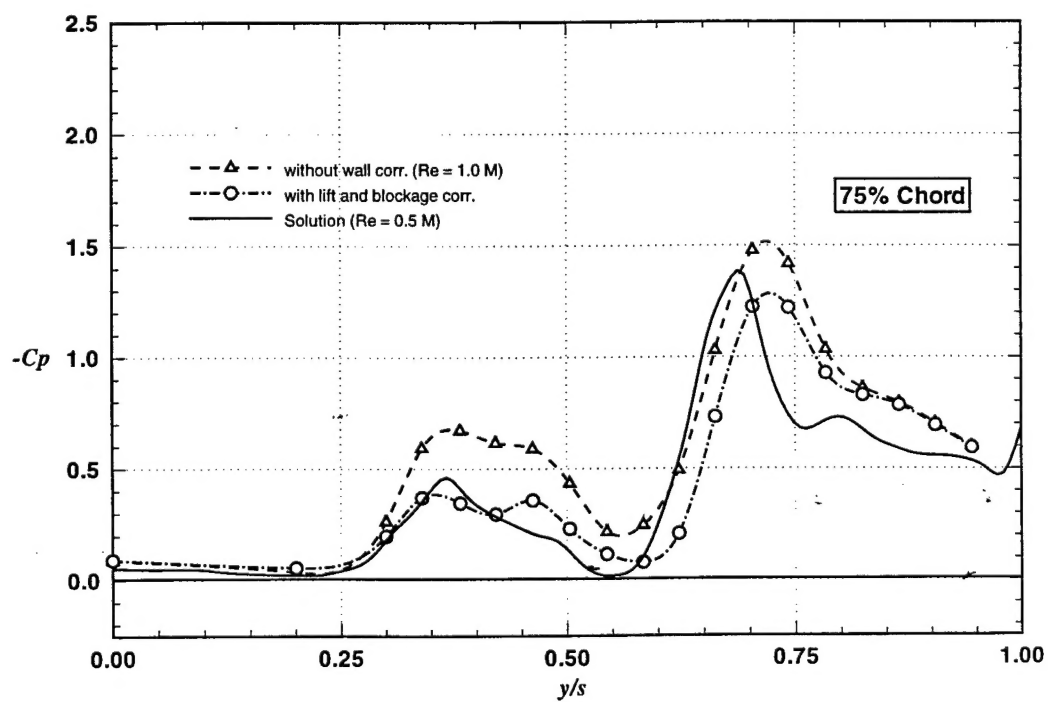
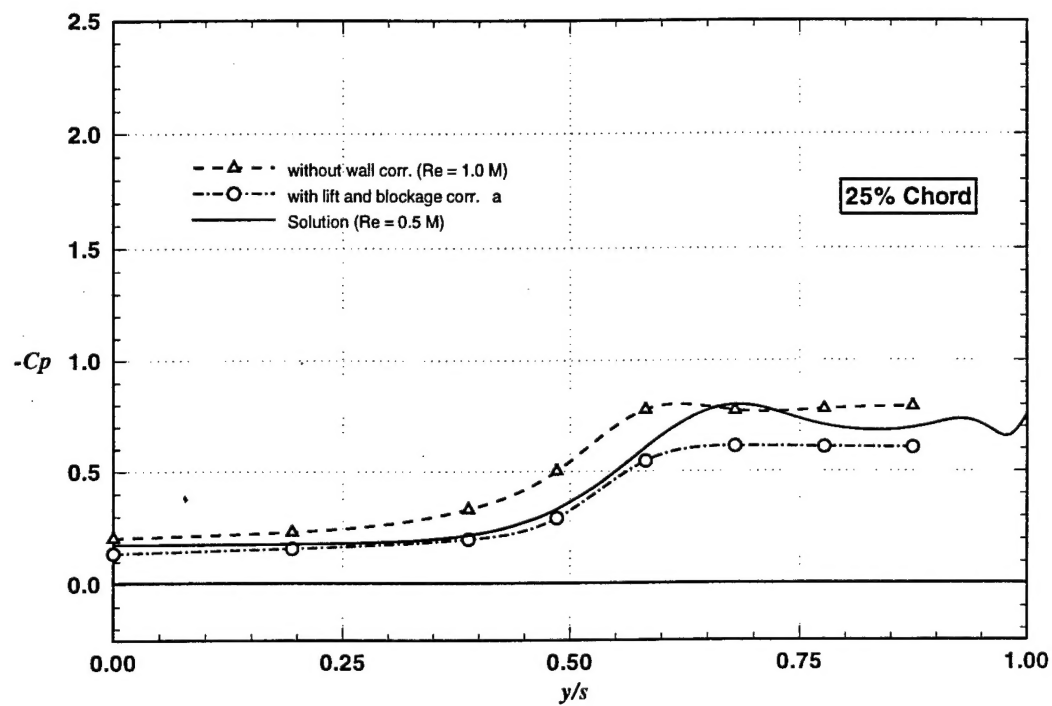


Figure 20: Comparison between solution and experiment;  $\alpha = 10$  deg